



DIPARTIMENTO DEL
TESORO

BTP Italia

Examples of Calculations

Calculation of the Indexation Coefficient, the coupons and the revaluation of principal (uplift)

This note provides information about the mechanism for computing the Indexation Coefficient (IC), and the calculation of the semi-annual coupon, the principal revaluation, and the semi-annual return yield by this security. Let's assume that an investor purchases a BTP Italia with a nominal value of €1,000, with first accrual date 1 March 2012, maturing on 1 March 2016 and with a real annual coupon rate of 2%. The following table shows the factors for the calculation of the Indexation Coefficient at a generic date starting from the first accrual date:

Date (d)	m-3	IstatIndex FOI (m-3)	m-2	IstatIndex FOI (m-2)	Days (in month m)	Day (d)	Reference IndexNumber (d,m)	Indexation Coefficient (IC)
01/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	1	104.00000	1.00000
02/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	2	104.01290	1.00012
03/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	3	104.02581	1.00025
04/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	4	104.03871	1.00037
05/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	5	104.05161	1.00050
06/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	6	104.06452	1.00062
07/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	7	104.07742	1.00074
08/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	8	104.09032	1.00087
09/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	9	104.10323	1.00099
10/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	10	104.11613	1.00112
11/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	11	104.12903	1.00124
12/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	12	104.14194	1.00136
13/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	13	104.15484	1.00149
14/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	14	104.16774	1.00161
15/03/2012	Dec-11	104.0	Jan-12	104.4	31.0	15	104.18065	1.00174

The calculation of the coefficient occurs daily by using the formula illustrated in the Explanatory Note. The following table illustrates the flow of the coupon payments and principal revaluation at each payment date, using the formulas illustrated in the Explanatory Note (assuming a constant annual inflation rate of 2%):



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Period	Reference Index Number	Indexation Coefficient	Coupon (€)	Principal Revaluation (€)	Semi-annual Return (€)
01/03/2012 Issuance	104.0	1			
01/09/2012 end of 1 st semi-annual period	104.7	1.00673	10.07	6.73	16.80
01/03/2013 end of 2 nd semi-annual period	106.1	1.01337	10.13	13.37	23.50
01/09/2013 end of 3 rd semi-annual period	106.8	1.0066	10.07	6.6	16.67
01/03/2014 end of 4 th semi-annual period	108.2	1.01311	10.13	13.11	23.24
01/09/2014 end of 5 th semi-annual period	108.9	1.00647	10.06	6.47	16.53
01/03/2015 end of 6 th semi-annual period	110.4	1.01377	10.14	13.77	23.91
01/09/2015 end of 7 th semi-annual period	111.1	1.00634	10.06	6.34	16.40
01/03/2016 end of 8 th semi-annual period	112.6	1.0135	10.14	13.5	23.64

In the case of deflation between one semi-annual period and the following, a floor to the Indexation Coefficient is used, and its use is illustrated below. The Treasury does not take devaluation into account, and sets a lower limit (floor) to the Indexation Coefficient, so that it cannot be less than one. The following table shows the assumption of deflation, with the adjustment of the Indexation Coefficient used for the calculation of the coupons, principal revaluation and the semi-annual return:

Period	Reference Index Number	IC	Adjusted Reference Index Number (floor)	Adjusted IC (floor)	Coupon (€)	Principal Revaluation (€)	Semi-annual Return (€)
01/03/2012 Issuance	104.0	1	104.0				
01/09/2012 end of 1 st semi-annual period	103.6	0.99615	104.0	1	10.00	0	10.00
01/03/2013 end of 2 nd semi-annual period	105.0	1.01351	105.0	1.00962	10.10	9.62	19.72
01/09/2013 end of 3 rd semi-annual period	104.7	0.99714	105.0	1	10.00	0	10.00
01/03/2014 end of 4 th semi-annual period	106.1	1.01337	106.1	1.01048	10.10	10.48	20.58
01/09/2014 end of 5 th semi-annual period	106.8	1.0066	106.8	1.0066	10.07	6.6	16.67
01/03/2015 end of 6 th semi-annual period	108.2	1.01311	108.2	1.01311	10.13	13.11	23.24
01/09/2015 end of 7 th semi-annual period	108.9	1.00647	108.9	1.00647	10.06	6.47	16.53
01/03/2016 end of 8 th semi-annual period	110.4	1.01377	110.4	1.01377	10.14	13.77	23.91

Finally, the table below shows the use of the floor to the Indexation Coefficient, under the assumption of a semi-annual period with deflation followed by another with positive inflation that is not high enough to recover the deflation of the previous one.

Period	Reference Index Number	IC	Adjusted Reference Index Number (floor)	Adjusted IC (floor)	Coupon (€)	Principal Revaluation (€)	Semi-annual Return (€)
01/03/2012 Issuance	104.0	1	104.0				
01/09/2012 end of 1 st semi-annual period	103.6	0.99615	104.0	1	10.00	0	10.00
01/03/2013 end of 2 nd semi-annual period	105.0	1.01351	105.0	1.00962	10.10	9.62	19.72
01/09/2013 end of 3 rd semi-annual period	104.7	0.99714	105.0	1	10.00	0	10.00
01/03/2014 end of 4 th semi-annual period	104.9	1.00191	105.0	1	10.00	0	10.00
01/09/2014 end of 5 th semi-annual period	106.8	1.01811	106.8	1.01714	10.17	17.14	27.31
01/03/2015 end of 6 th semi-annual period	108.2	1.01311	108.2	1.01311	10.13	13.11	23.24
01/09/2015 end of 7 th semi-annual period	108.9	1.00647	108.9	1.00647	10.06	6.47	16.53
01/03/2016 end of 8 th semi-annual period	110.4	1.01377	110.4	1.01377	10.14	13.77	23.91

Then, as it can be noted, the inflation of the fourth semi-annual period does not offset the deflation of the previous one and, therefore, the Indexation Coefficient in the fourth semester is once again equal to one.

Calculation of the nominal value of the BTP Italia revalued at a specific date

Let's assume that the investor purchases the BTP Italia with a nominal value of €1,000, first accrual date 1 March 2012, and maturing on 1 March 2016, and that the investor wants to calculate the revalued amount at 20 March 2012.

Thus, it is necessary to calculate the Indexation Coefficient of such date.

1. It is first necessary to calculate the base index number of the Indexation Coefficient which corresponds, at such date, to the index number of the first accrual date – 1 March 2012 (otherwise it corresponds to the date on which the last coupon was paid). The index number is obtained starting from the values of the FOI Istat Indices for the month that is three months prior to the month of March (December 2011) and the month that is two months prior to the month of March (January 2012).

- the value of the FOI Istat Index for the month of December 2011 is equal to 104;
- the value of the FOI Istat Index for the month of January 2012 is equal to 104.4.

The formula for the calculation of the index number (shown in the Explanatory Note) yields the following value (figuring the result with six decimals and then rounding to the fifth decimal):

$$\text{Index Number}_{01-03-2012} = 104 + \frac{1-1}{31} * (104.4 - 104) = 104$$

2. The index number as of the date of 20 March 2012 is then calculated.

This value is obtained starting from the values of the FOI Istat Indices for the month that is three months prior to the month of March (December 2011) and the month that is two months prior to the month of March (January 2012).

- the value of the FOI Istat Index for the month of December 2011 is equal to 104;
- the value of the FOI Istat Index for the month of January 2012 is equal to 104.4.

The formula for the calculation of the index number (shown in the Explanatory Note) yields the following value (figuring the result with six decimals and then rounding to the fifth decimal):

$$\text{Index Number}_{20-03-2012} = 104 + \frac{20-1}{31} * (104.4 - 104) = 104.24516$$

3. Finally, the Indexation Coefficient (IC) at 20 March 2012 is calculated by dividing the value of the reference index number obtained in point 2. by the value of the base index number obtained in point 1. (figuring the result with six decimals and then rounding to the fifth decimal):

$$\text{IC}_{20-03-2012} = 104. \frac{24516}{104} = 1.00236$$

Accordingly, as of 20 March 2012, the BTP Italia with a nominal value of €1,000 is revalued to €1,002.36.

Calculation of the payment flows based on different assumptions about the investor's behaviour

First of all, there are no fees due by the investor when purchasing the bond at issuance. The description below refers to coupon flows and to other forms of remuneration of the BTP Italia.

Two cases should be distinguished:

1. Purchase of the security at issuance and holding the security until maturity;
2. Purchase of the security at issuance and sale of the security on the secondary market before the final maturity.

1. Purchase of the security at issuance and holding of the security until maturity

In this case, the remuneration of the security (pre-tax) is the sum of the coupon interest, the semi-annual principal revaluation due to inflation and the bonus payment at maturity. The various components can be explained with an example. Let's assume that the investor purchases a BTP Italia with a nominal value of €1,000, first accrual date 1 March 2012, maturing on 1 March 2016 and with a real annual coupon rate of 2%.

The coupon payments and the principal revaluation at each coupon payment date are shown in the table below,

and are derived from the formulas illustrated in the **Explanatory Note** for this security:

Period	Reference Index Number *	Indexation Coefficient	Coupon (€)	Principal Revaluation (€)	Semi-annual Return (€)
01/03/2012 Issuance	104.0	1			
01/09/2012 end of 1 st semi-annual period	104.7	1.00673	10.07	6.73	16.80
01/03/2013 end of 2 nd semi-annual period	106.1	1.01337	10.13	13.37	23.50
01/09/2013 end of 3 rd semi-annual period	106.8	1.0066	10.07	6.6	16.67
01/03/2014 end of 4 th semi-annual period	108.2	1.01311	10.13	13.11	23.24
01/09/2014 end of 5 th semi-annual period	108.9	1.00647	10.06	6.47	16.53
01/03/2015 end of 6 th semi-annual period	110.4	1.01377	10.14	13.77	23.91
01/09/2015 end of 7 th semi-annual period	111.1	1.00634	10.06	6.34	16.40
01/03/2016 end of 8 th semi-annual period	112.6	1.0135	10.14	13.5	23.64

*Reference index number calculated on the basis of the assumption of annual inflation remaining constant at 2%

At maturity, an additional payment equal to 0.4% (pre-tax) of the nominal amount subscribed will be paid as a bonus¹. In the example considered, on 1 March 2016, the investor will receive a total of €1,027.64, inclusive of the reimbursement of the principal subscribed on 1 March 2012, the final semi-annual return flow, and the bonus payment.

2. Purchase of the security at issuance and sale of the security on the secondary market before the contractual maturity

In this case, the remuneration (pre-tax) is the sum of coupon interest and the semi-annual principal revaluation due to inflation.

As in the previous case, let us assume that the investor purchases a BTP Italia with a nominal value of €1,000, first accrual date 1 March 2012, maturing on 1 March 2016 and with a real annual coupon rate of 2%. However, instead of holding the security until maturity, the investor decides to sell it on the secondary market prior to the contractual maturity, for example, at the settlement date of 20 March 2014. It is also assumed that the sale price is equal to 100, namely, the price of issuance.

The coupon payments and the principal revaluation during the full semi-annual periods preceding the sale are the same as in the preceding example, whereas the value for the final period is calculated until the date of the settlement of the sale. The table illustrates the flows:

¹ Paid by the MEF to physical persons who purchase the bonds at issuance and hold them until maturity.

Period	Reference Index Number r^*	Indexation Coefficient	Coupon (€)	Principal Revaluation (€)	Semi-annual Return (€)
01/03/2012 Issuance	104.0	1			
01/09/2012 end of 1 st semi-annual period	104.7	1.00673	10.07	6.73	16.80
01/03/2013 end of 2 nd semi-annual period	106.1	1.01337	10.13	13.37	23.50
01/09/2013 end of 3 rd semi-annual period	106.8	1.0066	10.07	6.60	16.67
01/03/2014 end of 4 th semi-annual period	108.2	1.01311	10.13	13.11	23.24
20/03/2014 sale settlement	108.44516	1.00227	1.03	2.27	3.30

* Reference Index Number calculated on the basis of the assumption of annual inflation remaining constant at 2%

On 20 March 2014, the investor gets a total of €1,003.30, inclusive of the sale price and the coupon interest accrued between 1 March 2014 and 20 March 2014 and principal revaluation due to inflation.

In accordance with the calculation conventions and formulas shown in the Explanatory Note, the accrued coupon interest ($RC_{d,m}$) and the accrued principal revaluation ($RRC_{d,m}$) are equal to:

$$RC_{20-03-2014} = 0.02 \cdot \frac{19}{184} * 1,000 * 1.00227 = 1.0349$$

$$RRC_{20-03-2014} = 1,000 * \frac{100}{100} * (1.00227 - 1) = 2.27$$

where 19 is the number of days between 1 March 2014 and 20 March 2014; 184 is the number of days between 1 March 2014 and 1 September 2014, the latter being the contractual date for the payment of the next coupon; and 1.00227 is the Indexation Coefficient calculated as of 20 March 2014.

Please note that a fee may be charged for the sale of the security on the secondary market; the value of the fee is set by the bank where the investor holds his securities account.